Certificates for Verifiable Forensics

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Abstract—Digital forensics reports typically document the search process that has led to a conclusion; the primary means to verify the report is to repeat the search process. We believe that, as a result, the Trusted Computing Base for digital forensics is unnecessarily large and opaque.

We advocate the use of *forensic certificates* as intermediate artifacts between search and verification. Because a forensic certificate has a precise semantics, it can be verified without knowledge of the search process and forensic tools used to create it. In addition, this precision opens up avenues for the analysis of forensic specifications. We present a case study using the specification of a "deleted" file.

We propose a verification architecture that addresses the enormous size of digital forensics data sets. As a proof of concept, we consider a computer intrusion case study, drawn from the Honeynet project. Our Coq formalization yields a verifiable certificate of the correctness of the underlying forensic analysis. The Coq development for this case study is available at http://fpl.cs.depaul.edu/projects/forensics/.

I. INTRODUCTION

Eoghan Casey, editor-in-chief of *Digital Investigation*, a premier journal in computer forensics, recently editorialized [Casey 2012]:

Digital forensics can no longer tolerate software that cannot be relied upon to perform specific functions. The root of this problem is a lack of clearly defined software requirements, which compels users and tool testers to make educated guesses and assumptions about how we expect digital forensic tools to work. This makeshift approach results in untested errors in our tools that can lead to verdicts based on incorrect information and can damage the reputation of individual practitioners and the field as a whole.

The Scientific Working Group on Digital Evidence [2013] has raised similar concerns.

Why is unreliable software "intolerable" in a forensics context? In common practice, a forensics report is a narrative description of the search procedure: the report lists the tools that have been used and provides an argument for the conclusion based on the output of those tools. The validity of the conclusion depends upon the details of the process by which those conclusions are derived. If the tools that generate the output are buggy, then the conclusions themselves are in doubt. Unreliable software undermines the entire endeavor. Casey's argument is about poor tools, but the same argument can be applied to reasoning made outside the tools.

Rather than viewing this as a problem of software reliability, we view it as a problem of an overlarge Trusted Computing

Base (TCB). The problem is that the forensics argument is justified by the search process itself, rather than an independently verifiable conclusion. The TCB, therefore, must include all of the tools used during the search. The situation is particularly galling when the TCB must include tools that are monolithic and closed-source, as are many popular forensics applications. Projects such as NIST's Computer Forensics Tool Testing Program (http://www.cftt.nist.gov) have attempted to increase confidence in specific tools, but this approach inherits the usual limitations and difficulties associated with software testing.

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We have pursued an alternative approach familiar to the CSF audience: to reduce the size of the TCB. Our starting point is an analogy with certificates for SAT solvers: one should not trust the SAT solver that produces a certificate, only the verifier that checks it. We believe that the forensic search process should produce *forensic certificates* that precisely identify the data required to validate a conclusion, along with proof that the conclusion follows from that data. Unlike the forensic reports of current practice, forensic certificates can be verified without repeating the process of discovery.

In this paper, we summarize the challenges and the solutions we have discovered. The majority of our work is formalized in Coq; the development is available at http://fpl.cs.depaul.edu/projects/forensics/. Specifically, we have formalized parts of two submissions to the Honeynet Project forensics challenge [Honeynet Project 2001], by Matt Borland and Jason Lee. We describe our formalization of Borland's report in this paper. Further details may be found in Lubinski [2014].

A. Borland's Report

The forensic report by Matt Borland was one of the top five submissions to a Honeynet Project [Honeynet Project 2001] forensics challenge. The particular challenge was to identify a rootkit¹ within a Linux system. The evidence available to the participants was an image of the Ext2 file system. The reports for this challenge constitute informal, natural language arguments for an interpretation of data within the file system image.

Borland's challenge report states:

The rootkit was found on deleted inode 23 of the filesystem. It is a tar/gzipped file containing the tools necessary for creating a home for the attacker on the compromised system.

Due to evidence within the installation program contained within, I will call this rootkit 'lk.tgz.' Here are its contents:

drwxr-xr-x ... 2001-02-26 14:40:30 last/ -rwxr-xr-x ... 2002-02-08 07:08:13 last/ssh

¹A rootkit typically contains tools used to gain and maintain administrator or system privileges on a compromised machine.

```
-rw-r--r- ... 2001-02-26 09:29:58 last/pidfile
-rwx----- ... 2001-03-02 21:08:37 last/install
-rwx----- ... 2001-02-26 09:22:50 last/linsniffer
-rwxr-xr-x ... 1999-09-09 10:57:11 last/cleaner
-rw-r--r- ... 2001-01-27 09:11:32 last/inetd.conf
-rwxr-xr-x ... 2001-02-26 09:28:40 last/lsattr
-rw-r--r- ... 2001-01-27 09:11:44 last/services
-rwxr-xr-x ... 2001-02-26 09:22:55 last/sense
-rw-r--r-- ... 2000-10-22 14:29:44 last/ssh_config
-rw----- ... 2000-10-22 14:29:44 last/ssh_host_key
-rw-r--r- ... 2000-10-22 14:29:44 last/ssh_host_key.pub
-rw----- ... 2000-10-22 14:29:44 last/ssh_random_seed
-rw-r--r- ... 2001-02-26 09:29:51 last/sshd_config
-rwx----- ... 2001-02-26 09:22:59 last/sl2
-rwxr-xr-x ... 2001-02-26 09:23:10 last/last.cgi
-rwxr-xr-x ... 2001-02-26 09:23:33 last/ps
-rwxr-xr-x ... 2001-02-26 09:23:42 last/netstat
-rwxr-xr-x ... 2001-02-26 09:23:47 last/ifconfig
-rwxr-xr-x ... 2001-02-26 09:23:55 last/top
-rwx----- ... 2001-02-26 09:24:03 last/logclear
-rw-r--r- ... 2001-03-02 21:05:12 last/s
-rwxr-xr-x ... 2001-02-26 08:46:04 last/mkxfs
```

I used icat to extract the first file, specifying the inode using the following commands:

\$ icat honeynet/honeypot.hda8.dd 23 > recovered/file-23
Then using 'file,' I am given a guess at the type of
file.

```
$ file recovered/file-23
recovered/file-23: gzip compressed data, deflated,
  last modified: Fri Mar 2 21:09:06 2001, os: Unix
```

At this point, I could then say: \$ tar tzvf recovered/file-23

Which then lists the contents of the tar/gzipped file, which in this case returns the listing I included in my analysis of the rootkit.

This inclusion of tool names, input parameters and output is typical of forensic reports. In general, these tools interpret data structures or search for data. The report does not always contain the entire output from the tool; it is implicit that the omitted output is irrelevant.

Borland's report uses ils from The Coroner's Toolkit to list the inodes of deleted files, ils2mac to translate the output, and mactime to extract access times for the inodes of deleted files.

```
# ils honeynet/honeypot.hda8.dd > ilsdump.txt
# ils2mac ilsdump.txt > deleted.txt
# mactime -p ../hp/etc/passwd -b deleted.txt 1/1/2001
```

This kind of tool composition is also typical. Here, the output of ils is fed to mactime. The examiner must also massage the data from one format to another using ils2mac to accommodate the ad hoc formats used by these tools. DFXML has been proposed as a standard format to simplify this kind of composition [Garfinkel 2012].

The report also includes expert interpretation. For example, the contents of the /root/.bash_history file suggest that new software was installed.

```
mkdir /var/...; cd /var/...
ftp ftp.home.ro
tar -zxvf emech-2.8.tar.gz
cd emech-2.8
./configure; make; make install
/mach/mach/
```

Knowing that /var is traditionally mounted on a separate partition, this information is used in conjunction with the earlier timestamp investigation to form a hypothesis about the intruder's activities:

```
...their ftp to ftp.home.ro would explain the ~7 minutes between login at 8:45 and change of /etc/ftpaccess at 8:52...
```

Borland's report demonstrates the challenges involved in: (a) identifying the precise semantics of tools and natural language statements; and (b) independently verifying the behavior of tools, their composition, and arguments involving expert interpretation.

B. Formalizing Borland's conclusion

Borland's primary conclusion is that there is a deleted file on the disk that, when uncompressed, looks like a rootkit. Thus, our primary definition in Coq is a predicate that explains what has been found in a file system image:

```
Definition borland_rootkit (img : Img) : Prop :=
  exists (file : File),
   isOnDisk file img
  /\ isDeleted file
  /\ isGzip file img
  /\ Tar.looksLikeRootkit (gunzip file img).
```

This predicate indicates that (a) the file is found on the image img, (b) the file is deleted, (c) the contents of file is gzip-compressed, and (d) when decompressed, the result is a tar archive that is consistent with a rootkit. For this final predicate, Borland described the contents of the archive as containing "necessary" files for a rootkit installation; we used the list of names he provided in our formalization of looksLikeRootkit.

While file systems must have clear semantics for non-deleted files, heuristics for recovery of deleted files are often poorly specified. Fortunately, deletion in an Ext2 file system is not destructive; the inode is simply marked as unused, and its link count zeroed. Therefore, we were able to use a very simple predicate for isDeleted. We discuss the greater issues in section VI.

The primary challenge of the formalization lies with the large volume of data common to digital forensics. The Ext2 file system image from the Honeynet challenge is 259MB. This is an unusually small file system. Nevertheless, it is too large to load into traditional theorem provers.

To gain a sense of the size limitations in existing theorem provers, consider the representation of file system images as maps using AVL trees from the Coq standard library, with binary integers for the keys and values in the map. In this representation, creating and looking up a single element in the map $\{n \mapsto n \mid 0 \le n \le 10^4\}$ takes ~10 seconds and 400MB of RAM to compute, and the same operations for the map $\{n \mapsto n \mid 0 \le n \le 10^5\}$ take ~180 seconds and 1.2GB of RAM.

This prompts the question, is it possible to identify a subset of the file system image that justifies the forensic claim and can be reasoned about using a theorem prover? And, if so, is it sound to conclude that the forensic claim holds for the entire file system image when it holds for the subset?

In many cases, the answer to both is yes. For example, consider a statement that a file exists within a file system image. The subset of the image required includes file system metadata and the sequence of directory entries leading to the file. We describe this form of reasoning in section III.

In the case of the Honeynet challenge, our case study shows that Borland's forensic claim can be justified using a subset of ~2,400 bytes from the file system image, declared as follows (offset 1,024 is the beginning of the superblock):

```
Definition honeynet_partial : Map_N_Byte := [
  1024 |-> ("216":Byte), 1025 |-> ("002":Byte), ...
]
```

Our main result, then, is predicated on the assumption that honeynet_partial \sqsubseteq honeynet_img

where □ is the subset ordering on maps represented as functions. To make use of this inclusion, the predicates in the forensic claim must be monotone with respect to □. More complex strategies must be adopted to reason about non-monotonic predicates, e.g., "there is no file named heist.doc" or the more subtle "there are precisely 3 web pages in the browser cache that refer to the heist".

Similar difficulties arise with decompression. It is certainly possible to formalize gunzip in Coq, but in practice this is unattractive due to the volume of data involved. Instead, the main theorem uses a second map, gunzipped_partial, and postulates the relationship

 ${\tt gunzipped_partial} \ \sqsubseteq \ {\tt gunzip} \ {\tt disk} \ {\tt file23}$

where file23 is bound to the particular deleted inode where the rootkit was found.

Our formalization then consists of Coq proofs in addition to two verifications that are conducted outside Coq: (a) that honeynet_partial is a subset of the entire file system image, and (b) that gunzipped_partial is a subset of the content obtained by decompressing file23.

With these techniques, we have been able to provide a formal, verifiable interpretation of Borland's report.

C. Contributions

In this paper, we report the following contributions:

- A general framework for the representation and verification
 of forensics certificates. The architecture is discussed in
 the next section, techniques for scaling to large data sets
 in section III, and generation of compact Coq proofs in
 section IV.
- A case study formalization of Borland's report for the Honeynet challenge, which we describe in more detail in section V.
- A novel approach to the specification and analysis of forensic data-recovery heuristics based on providing patches that restore data structures, presented in section VI.

We discuss related work in section VII.

II. ARCHITECTURE FOR FORENSIC CERTIFICATES

Our approach to obtaining sound, reproducible results is based on the idea of forensics search tools producing forensic

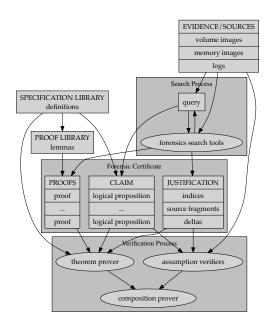


Figure 1: Architecture

certificates that are verified by independent software. Importantly, the verification of a forensics certificate can be conducted:

- after the search has been completed, both by the creator of the certificate and by independent experts during subsequent legal proceedings,
- without access to the search software,
- with alternative specification libraries, and
- more efficiently than the original search.

The architecture is depicted in Figure 1. We discuss each major component below.

Search process: The search process operates on a collection of evidence/sources such as media images containing volumes or file systems, memory images, log files, etc. An investigator develops a query and executes search tools iteratively, refining the query based on search results.

The search process yields a claim that is supported by justifying data identified during the search, as well as proofs. We refer to the composite object as a forensic certificate. We now consider each component of the forensic certificate.

Forensic Certificate: Claim: The claim is an assertion about the evidence. We give three simple examples:

- (a) a file exists at an absolute path within a file system
- (b) a deleted file exists within a file system
- (c) there are no occurrences of a particular file within a file system (deleted or otherwise)

The meaning of (a) is clear. The meaning of (b) is uncertain, because there is no canonical definition of what it means to be a deleted file in a file system. In fact, different tools use different definitions [Casey 2004]. Unlike (a) and (b), (c) is

a negative assertion, and can only be validated by examining much of the file system image. However, the scope of the examination is ambiguous, because of the ambiguity of what it means to be a deleted file. We discuss the variety of claims for deleted files in more detail in section VI.

We require claims to be formalized in an appropriate logic. This formalization acts as an *unambiguous interface*, and thus facilitates a clear separation between search and independent verification of results.

Forensic Certificate: Justification: A naive approach to verifying a claim is to execute a second search using alternative trusted software, and compare the results with the original claim. This is the approach taken by traditional testing, e.g., http://www.cftt.nist.gov. In addition to the obvious problems with this technique (availability of alternate tools, need to compare output with potentially different semantics, etc), it is also inefficient. Efficiency can be improved by insisting that search software identifies the values that justify claims. For example, if a deleted file is claimed, the location of the file contents and/or a directory entry must be provided as a justifying value. Thus the problem is shifted from one of search to one of verification of a claim with justifying values.

Our insight is that the justifying values arise as witnesses for existential quantifiers and disjunctions in logical specifications of data structures such as file systems. For example, a logical formula for "a file exists within a file system" would include existentials representing the location of the file's content and the location of the directory entry for the file, amongst other metadata structures. Thus logical specifications provide a design criterion for the justifying data that is used to verify a search result. This becomes more significant as the complexity of file system structures grows.

Justifying data need not be limited to parts of the original evidence, but may also include information found during computational search. Such justifying data includes parameters such as reconstructed RAID parameters and recovered passwords / keys. More complex examples are possible. For instance, one may provide a file that is consistent with a remnant (such as a hash or file fragment) found in the evidence.

The information in DFXML output from forensics search tools can be seen as justifying values [Garfinkel 2012]. Without a guiding conclusion, however, it is not clear what part of the output is important. In the process of developing a standalone verifier for DFXML output with the NTFS file system, we discovered that some required values were not included. (DFXML only lists the first MFT entry for each file, but there could be many for a single file.)

Forensic Certificate: Proofs: It is possible to write direct verifiers for families of claims and justifying values, but such verifiers inherit the complexity of the data structures (and their specifications), and there is no a priori reason to trust that they are correct. Instead we require claims to be verified using a theorem prover. Semi-automated theorem proving systems such as Coq, Isabelle, etc., allow users to prove theorems interactively. We avoid this mode of operation, and instead require that a forensic certificate includes a proof of each component of the claim, using the justifying values as witnesses. Proofs are specific to a particular theorem prover,

but justifying values are not. Proofs may use lemmas from a proof library, which is not part of the TCB because the proofs in the library can be verified. We discuss methods for creating proofs in section IV.

Specification Library: The specification library provides logical specifications of data structures for, e.g., file systems, volume systems, or memory images. In particular, the specifications extend to partially-corrupted data structures, such as definitions for remnants of a deleted file existing in a file system. In such cases, there are often alternative definitions. Making these definitions precise resolves ambiguity in forensic search tools. We discuss reasoning about the correctness of definitions in the specification library in section VI.

Verification Process: Theorem Prover: The theorem prover takes as input logical formulas from the claim as well as the proofs with justifying values. The prover verifies the proof without human input. If the verification of the proof fails, the forensic certificate is rejected. Formulas within the claim can be verified independently of one another, facilitating parallel or randomized testing of proofs within a set of results where desirable. Note that the verification process does not require access to the forensic search tools used to generate the forensic certificate.

Perhaps surprisingly, the theorem prover does not use the evidence directly: existing theorem provers are unable to manage the quantity of data found in typical evidence. Instead we rely on the search process to identify fragments of the evidence that are relevant to particular propositions in a claim. The theorem prover manipulates fragments instead of the original evidence. These fragments are part of the justifying values in the forensic certificate.

Although the architecture is not tied to a particular theorem prover, we have used Coq. Thus our claims are written in a typed, higher-order logic, and proofs are represented as proof terms. We use computational reflection as a strategy for generating compact proofs. See section IV.

Verification Process: External Assumption Verifiers: To detect accidental or deliberate inaccuracies in the fragments, the verifier must also establish the that the fragments of evidence used by the theorem prover are consistent with the original evidence. The task is ill suited to general purpose theorem provers due to the large quantity of data. We therefore verify the relationship between fragments and the original sources with separate tools. We refer to these tools as external verifiers, because they verify propositions, from the claim, that are assumptions (hypotheses) for the forensic claims verified by the theorem prover. The external verifiers make use of justifying values and the original evidence.

There are many verification tasks with similar qualities, e.g., calculating cryptographic hashes of part of a media image; scanning a media image to identify all occurrences of regular expression matches; etc. Our architecture permits the introduction of an external verifier for each task.

By design, this part of the verification is low complexity (e.g., testing whether the fragment is a contiguous subsequence of an original media image). Nevertheless, the assumption verifiers are part of the TCB. Confidence in these verifiers can be established using standard program verification techniques.

Verification Process: Composition Verifier: The verification of a forensic certificate is divided between the theorem prover and external verifiers for reasons of scale and efficiency. To ensure validity of the final conclusion, additional deductions must be verified. These simple first-order deductions can be verified using a theorem prover that is specialized to reason about large data. The use of a separate composition verifier avoids the need to modify the proof-checking kernel of a sophisticated theorem prover such as Coq.

III. FEASIBILITY OF FORMAL FORENSICS

The simplest formal model of data forensics assumes that evidence can be referenced directly in formulas used by a theorem prover. However, such a simple model is infeasible in an unmodified prover due to the size of the data to be examined. While it is possible to modify a prover to provide efficient access, this would require modifications to the trusted verifier core of existing provers, prompting soundness concerns.

Instead, as described in the previous section, we factor verification between a base verifier (such as Coq) and external verifiers. The external verifiers are trusted to approve or repudiate statements of the base logic without formal proof. The external verifiers are designed to efficiently check properties of large data sets (for example, that certain bytes are present at certain addresses). Results from the base verifier and external verifiers are designed to be easy to compose with simple first-order deduction.

A. Reasoning via Bounds

Let Img be a map from offsets to bytes, representing a file system image. Suppose a search tool identifies that property ϕ holds for Img. Let img be a fresh variable and let ϕ' be the formula obtained by replacing all occurrences of Img by img in ϕ ; thus $\phi = \phi'[\text{img} := \text{Img}]$. Since Img is large in almost all forensic applications, the formula ϕ will be too large for existing theorem provers, even when ϕ' is small.

Many properties of interest in digital forensics do not require that the entire image be examined. For example, file identification tools often inspect only a few bytes at the start or end of a file. Similarly, affirming the existence of a file with a given pathname requires checking the bytes in a sequence of directory entries and some metadata.

We therefore adopt *partial* maps as our standard representation of disk images and seek to keep these as small as possible. We rely on forensics search tools to isolate the submap $\operatorname{Bnd} \sqsubseteq \operatorname{Img}$ that is relevant to the property of interest. As usual, the notation $b \sqsubseteq i$ indicates that when b is defined it agrees with i and that b is undefined whenever i is undefined. The proof for ϕ then consists of the following three components (recall that $\phi = \phi'[\operatorname{img} := \operatorname{Img}]$):

$$\forall \mathsf{img.} \; (\mathsf{Bnd} \sqsubseteq \mathsf{img} \Rightarrow \phi') \tag{1}$$

$$\mathsf{Bnd} \sqsubseteq \mathsf{Img}$$
 (2)

$$\{\forall, \Rightarrow\}$$
-elimination to conclude ϕ (3)

If both Bnd and ϕ' are small, then (1) is small, and therefore it can be checked by the base verifier. Since (2) includes

Img, this formula must be checked by an external assumption verifier. Trust in the external verifier must be established separately. The decision procedure for map inclusion is extremely simple, therefore standard program verification techniques can be applied to the external verifier without great cost. The deduction (3) is a first-order deduction carried out by the composition verifier.

Monotonicity: Often, formula (1) above can be established by demonstrating that ϕ' is monotone with respect to \sqsubseteq and then establishing $\phi'[\mathsf{img} := \mathsf{Bnd}]$. That is, the following statements are established in the base verifier, then (1) is deduced.

• Monotonicity of ϕ' :

```
\forall \mathsf{img}_1, \mathsf{img}_2. \ (\mathsf{img}_1 \sqsubseteq \mathsf{img}_2 \land \phi'[\mathsf{img} := \mathsf{img}_1] \Rightarrow \phi'[\mathsf{img} := \mathsf{img}_2])
```

• ϕ' is shown to hold for Bnd: ϕ' [img:= Bnd]

Example III.1 (Monotonicity of Parsing Ext2 Superblocks). Monotonicity results are often obtained compositionally, and the intermediate results may have additional quantification. For example, the procedure to compute a superblock record from an Ext2 file system image is monotone in the image. This is captured in the following Coq lemma from our Honeynet development (where the Found constructor indicates a successful operation):

B. Spatial Decomposition

A search for documents in a file system often produces thousands of files. In such cases, the claim for a forensics search yields a formula that is too large to represent in existing theorem provers such as Coq. Fortunately, forensics search results are often naturally represented as conjunctions of subformulas that refer to distinct areas of an image. Subformulas are checked by the base verifier, and conjunctions of those subformulas are checked by the simpler composition verifier, facilitating, e.g., parallel or randomized verification of components of forensics results.

Consider a statement $\phi \triangleq \bigwedge_{i \in I} \phi_i$, where Img appears in each subformula ϕ_i . As an example of such a statement, each ϕ_i may describe the existence of a file in Img. Assume a family of partial maps (Bnd_i | $i \in I$) and formulas (ϕ'_i | $i \in I$) such that $\phi_i = \phi'_i$ [img:=Img], each ϕ'_i contains no occurrences of Img, and each ψ_i is provable with the base verifier, where:

$$\psi_i \stackrel{\triangle}{=} \forall \text{img} : \text{map. } (\mathsf{Bnd}_i \sqsubseteq \mathsf{img} \Rightarrow \phi_i') \qquad (\forall i \in I)$$

Now the size of the conjunction $\bigwedge_{i \in I} \psi_i$ may still be too large for the base verifier because of the size of $\Sigma_{i \in I} |\mathsf{Bnd}_i|$. For example, if ϕ_i represents a statement about the contents of a file in a file system, then each Bnd_i could be the entire file contents. Moreover, if I ranges over all files within a file system, then the size of the statement $\bigwedge_{i \in I} \psi_i$ is linear in the size of the allocated space within the file system. For this

reason, the final deduction of ϕ must be performed by the composition verifier.

The proof for ϕ then consists of three components:

$$\forall \mathsf{img.} \ (\mathsf{Bnd}_i \sqsubseteq \mathsf{img} \Rightarrow \phi_i') \qquad (\forall i \in I) \tag{4}$$

$$\mathsf{Bnd}_i \sqsubseteq \mathsf{Img} \qquad (\forall i \in I) \tag{5}$$

$$\{\forall, \Rightarrow\}$$
-elimination and $\{\land\}$ -introduction to conclude ϕ (6)

Again (4) is checked by the base verifier, (5) by an external verifier, and (6) by the composition verifier.

More generally, it may not be possible to find small partial maps as above. For example, consider the statement that a directory exists at an absolute path $/d_0/d_1/.../d_{N-1}$. If ϕ_i' states that there is a directory entry with name d_i and a path from the root directory, then establishing ϕ_i' requires additional bounds on img:

$$\forall \text{img} : \text{map.} \ (\bigwedge_{0 \le j \le i} \text{Bnd}_j \sqsubseteq \text{img}) \Rightarrow \phi_i') \qquad (\forall i \in I)$$

However, $\Sigma_{0 \le j \le i} |\mathsf{Bnd}_j|$ may be too large. Instead, we establish ϕ as above, replacing (4) with:

$$\forall \mathsf{img.} \ ((\bigwedge_{0 \leq j \leq i-1} \phi_j' \land \mathsf{Bnd}_i \sqsubseteq \mathsf{img}) \Rightarrow \phi_i') \quad (\forall i \in I) \quad (7)$$

Note that the upper bound on j is i-1, rather than i. Perhaps unusually, this application of cut serves to reduce the size of the formulas under consideration rather than the size of proofs.

C. Sound and Complete Search Results

Consider a forensics search for a set of offsets X satisfying a property P, e.g., occurrences of regular expression matches. Here we consider proofs that:

- (a) each offset in X satisfies P (soundness), and that
- (b) X contains every offset satisfying P (completeness).

Soundness: We must establish that each offset in X satisfies P. Let dom(Img) = [0,N) for some N. The soundness of the search can be expressed as follows.

$$\phi \stackrel{\scriptscriptstyle\triangle}{=} \forall n, 0 \le n < N \Rightarrow (n \in X \Rightarrow P(\mathsf{Img}, n))$$

As before, we assume partial maps $(Bnd_n \mid n \in X)$ such that the following is provable with the base verifier:

$$\forall \text{img. Bnd}_n \sqsubseteq \text{img} \Rightarrow P(\text{img}, n) \qquad (n \in X)$$

Now $\Sigma_{n \in X} |\mathsf{dom}(\mathsf{Bnd}_n)|$ may be large, so the base verifier cannot generally deduce:

$$\forall \mathsf{img.} \ (\bigwedge_{n \in X} (\mathsf{Bnd}_n \sqsubseteq \mathsf{img})) \Rightarrow \\ \forall n, 0 \le n < N \Rightarrow (n \in X \Rightarrow P(\mathsf{img}, n))$$

Instead, we use the base verifier to establish that individual results about each Bnd_n , for $n \in X$, can be combined using formula ξ below. The complexity of ξ arises from the quantification over bounds used for partial maps (eliminated in the subsequent composition verifier deduction). The complexity is justified by the reduction in size of the formula presented to the

base verifier, and by the simplicity of the composition verifier. The proof for soundness has the following steps:

$$\forall \text{img. Bnd}_n \sqsubseteq \text{img} \Rightarrow P(\text{img}, n) \qquad (n \in X)$$
 (8)

$$\forall (\mathsf{bnd}_n \mid n \in X). \\ (\bigwedge_{n \in X} (\forall \mathsf{img. bnd}_n \sqsubseteq \mathsf{img} \Rightarrow P(\mathsf{img}, n))) \Rightarrow \\ \forall \mathsf{img. } ((\bigwedge_{n \in X} \mathsf{bnd}_n \sqsubseteq \mathsf{img}) \Rightarrow \\ (\forall n. \ n \in X \Rightarrow P(\mathsf{img}, n)))$$
 (9)

$$\mathsf{Bnd}_n \sqsubseteq \mathsf{Img} \qquad (n \in X) \tag{10}$$

$$\{\forall, \Rightarrow\}$$
-elimination and $\{\land\}$ -introduction to conclude ϕ (11)

Here (8) and (9) can be checked by the base verifier, (10) by the external verifier, and (11) by the composition verifier.

Completeness: Now we must establish that every offset satisfying P appears in X:

$$\phi \stackrel{\triangle}{=} \forall n. \ 0 \le n \le N \Rightarrow (P(\mathsf{Img}, n) \Rightarrow n \in X)$$

Since the entirety of Img must be examined in general, e.g., for regular expression matches, it is unlikely that small partial maps can be used directly for such proofs. Instead we consider how to use assumptions about intervals where the property P does not hold. This is useful when the number of intervals is significantly smaller than the total size of the intervals. The assumptions must be checked using external verifiers that understand P.

To illustrate, consider a family of pairs $I \subset \mathbb{Z} \times \mathbb{Z}$ representing the intervals where P does not hold, i.e.:

$${n \mid (x,y) \in I \land x \leq n < y} = dom(Img) \setminus X$$

We use trusted external verifiers to check the family of results:

$$\forall n. \ x \le n < y \Rightarrow \neg P(\mathsf{Img}, n) \qquad ((x, y) \in I)$$

Then the proof for completeness consists of:

$$\forall \text{img. } (\bigwedge_{(x,y) \in I} (\forall n. \ x \le n < y \Rightarrow \neg P(\text{img}, n))) \\ \Rightarrow \forall n. \ 0 \le n < N \Rightarrow (P(\text{img}, n) \Rightarrow n \in X)$$
 (12)

$$\forall n. \ x \le n < y \Rightarrow \neg P(\mathsf{Img}, n) \qquad ((x, y) \in I) \tag{13}$$

$$\{\forall, \Rightarrow\}$$
-elimination and $\{\land\}$ -introduction to conclude ϕ (14)

(12) is checked by the base verifier, (13) by an external verifier, and (14) by the composition verifier. The proof of (12) uses the fact that:

$$\forall n. \ 0 \le n < N \Rightarrow n \in X \lor (\bigvee_{(x,y) \in I} x \le n < y).$$

Example III.2 (Counting Deleted Files). Consider a forensic claim that there is exactly one deleted file in an Ext2 file system image. To make "deleted" precise, we mean that there is an inode with a link count of zero [Carrier 2005]. The link count is stored in 2 bytes within an inode. The Ext2 Honeynet image has 66,264 inodes, and so the naive formalization that uses a subset of the file system image with all inode link counts requires a partial map with 132,528 entries, which is large enough to be problematic in a theorem prover.

Fortunately, inodes are stored consecutively within a small number of block groups, and this can be used to reduce the size of the partial map used within a theorem prover. First, define the predicate $\phi(\text{img}, s, m, n, v, X)$ so that X is the set of offsets in s, s+m, s+2m, ..., s+(n-1)m, where a value v occurs in two bytes within img. That is:

$$\begin{aligned} \phi\left(\mathsf{img}, s, m, n, v, X\right) &\stackrel{\triangle}{=} \\ X &= \big\{ j \mid 0 \leq j < n \\ & \land \mathsf{img}[s+j*m] + 256* \mathsf{img}[s+j*m+1] = v \big\} \end{aligned}$$

A simple external verifier can be constructed to verify ϕ .

For the Honeynet challenge image there are 2,008 inodes per block group, and suppose that s_0 , s_1 , s_2 , ..., s_{32} are the offsets for the inode tables within each block group. There are 128 bytes per inode, and the link count is stored in offsets 26-27 within an inode. If the forensic claim is that the deleted file occurs in the 20th inode of block group zero, the hypothesis used within the theorem prover is then:

```
\phi(\text{img}, s_0 + 26, 128, 2008, 0, \{19\}) \land \phi(\text{img}, s_1 + 26, 128, 2008, 0, \{\}) \land \phi(\text{img}, s_2 + 26, 128, 2008, 0, \{\}) \land \dots 
 \phi(\text{img}, s_{32} + 26, 128, 2008, 0, \{\})
```

With the above hypothesis, the definition of ϕ , and file system metadata from the superblock, it is possible to establish that there is exactly one deleted file. With this approach, the resulting formula for the forensic claim is linear in the number of block groups (33 in the Honeynet example), as opposed to being made linear in the number of inodes (66,264 in the Honeynet example) by the large partial map.

D. Composition Verifier

The arguments above, in (3), (6), (11) and (14), demonstrate that, by design, results from the base verifier and external verifiers can be composed using propositional reasoning and ∀-elimination. We leave the implementation of such a composition verifier to future work, but note that it is far simpler than the kernels of theorem provers for more sophisticated logics. The only interesting detail is that the composition verifier must have native support for the large maps arising from file system images, memory images, etc. For example, formulas might refer to the names of files containing the large maps, as opposed to having the large maps embedded within the formulas.

IV. GENERATION OF PROOFS

An important design principle for the architecture is that generation of forensic certificates must be automated, and must not require additional effort by forensic examiners. Forensic certificates contain justifying data, claims, and proofs. Existing forensic search tools often produce enough information to create the first two via an automated post-processing step, given sufficient knowledge of the search tools' behaviour. Formal proofs however are more difficult to recreate from the output of forensic search tools. In addition, the size of

proofs must be minimized, as discussed in section III. Here we illustrate the issues using the Coq theorem prover, and outline how to generate compact proofs using a proof by reflection strategy.

Coq is a semi-automated type-checker for a powerful dependently-typed programming language, and is used as a theorem-proving framework. Although proof terms in Coq can be written directly, they are often constructed using a tactic language. A proof term constructed by tactics is type-checked, or verified, and can be saved for subsequent standalone verification.

Thus there are two competing methods for distributing proofs. The first is to distribute the tactics script, which is often easier to understand or modify than a proof term; however, verifying the script is potentially expensive because it entails repeating the same proof search, and tactics are less robust than proof terms because of the potential for changes in the proof search algorithms. The second method is to distribute the proof term. For the content of forensic certificates, the second method is preferable because of the potential inefficiency and non-robustness of tactic scripts.

It remains to generate the proof term to be stored in the forensic certificate. One approach is to develop custom tactics that are specific to the claims produced by forensic search tools. The custom tactics conduct an automated proof search on behalf of the forensic examiner. Following the original design principle, custom tactics are expected to find a proof if one exists, so that the forensic examiner need not be involved with the theorem prover.

Our experiments suggest that proof search for forensic claims is challenging to execute efficiently, and easily leads to proof terms that are too large to type check with Coq. In particular, the size of proof terms can be proportional to the number of cases in a proof, and naive proofs about forensic claims do generate very large numbers of cases.

A. Proof by Reflection

Rather than use tactics based search, we have adopted a *proof by reflection* strategy for the generation of proof terms. Proof by reflection Harrison [1995] replaces a proof search with a computational procedure, when the computational procedure has been proven correct.

Proof by reflection relies on the following type inference rule. It allows a term M to be type checked with type U if M has type T and the types T and U are convertible.

$$\frac{\Gamma \vdash M : T \qquad T \equiv U}{\Gamma \vdash M : U}$$

The convertibility relation includes computation. For example, consider a boolean-valued function f. The previous typing rule can be instantiated to show that the proof term for reflexivity of equality eq_refl has type f x = true whenever $true \equiv f x$, i.e., when executing f x results in true.

$$\frac{\Gamma \vdash \texttt{eq_refl:true} = \texttt{true} \quad (\texttt{true} = \texttt{true}) \equiv (\texttt{f x} = \texttt{true})}{\Gamma \vdash \texttt{eq_refl:f x} = \texttt{true}}$$

Suppose additionally that it is possible to deduce a property $P \times F$ from the computation of $f \times F$ returning true, written:

```
\Gamma \vdash \mathtt{sound} : \forall \mathtt{x}, \mathtt{f} \ \mathtt{x} = \mathtt{true} \rightarrow \mathtt{P} \ \mathtt{x}
```

With this form of lemma, f can be seen as certified code for the property P, and, if the reverse implication holds, a decision procedure for P.

The impact of having a computational procedure f is that a proof of P v, for some literal value v, has a simple tactics script of the following form. It uses the sound lemma, and then checks that computing f v yields true.

```
Lemma result : P v.
Proof.
apply sound; reflexivity.
Qed.
```

B. Application to Forensic Certificates

In the context of forensic certificates with large sources and the limitations of existing theorem provers, the size of the tactics script is less important than the size of the corresponding proof term that it creates. In the case of result above, the proof term is:

```
sound v (@eq_refl bool true)
```

In particular, for forensic claims, the literal value v may be a large fragment of a disk image. Naive proof terms generated by custom tactics can have size that is quadratic or worse in the size of v, and so the single occurrence of v in the proof term above is a significant improvement.

In addition to decreasing the size of proof terms, our experiments suggest that it is easier to develop computational procedures than custom tactics for proving forensic claims. Moreover, the procedures are for verification of justifying data from a forensic certificate, as opposed to searching for the same data, and so the procedures are simpler than forensic search tools. However, the procedures to be developed even for simple file system claims have more variety than the code found in a file system driver, because they may verify properties of partially-corrupted data structures, e.g., for verifying claims about deleted files.

The correctness of the computational procedures is established by lemmas such as sound above. This allows the specification for forensic claims to be defined via, e.g., a graph logic statement encoded in Coq, rather than via a reference implementation. The former is more convenient for the type of analysis discussed in section VI.

Finally, the use of computational procedures for verifying forensic certificates facilitates reasoning about the completeness of the procedure, as opposed to custom tactics. This can remove the risk that a forensic search produces a claim that cannot be proven despite testing of the process to generate a proof.

C. Runtime Performance

To verify each proof in a forensic certificate, the theorem prover must re-execute the computational procedure. For this reason, we must pay attention to the efficiency of reduction in theorem provers. Our experiments in this area suggest that, with care, the Coq theorem prover can perform computations for our formalization of a forensics challenge from the Honeynet project within a few seconds. In section VII we discuss related work on increasing runtime performance necessitated by the use of a proof by reflection style.

V. CASE STUDY: COMPUTER INTRUSION

In this section, we return to our formalization of Matt Borland's forensic report for one of the Honeynet Project's challenges [Honeynet Project 2001]. The formalization involves verification of results using both Coq and external verifiers, in addition to deduction between the components as discussed in section III. The following discussion reflects the fact that almost all of the development effort lay in the specification and verification using Coq.

The Coq development for this case study is available at http://fpl.cs.depaul.edu/projects/forensics/.

A. Forensic Claim

Recall the Coq definition of the predicate for the claim of Borland's report:

```
Definition borland_rootkit (img : Img) : Prop :=
  exists (file : File),
   isOnDisk file img
  /\ isDeleted file
  /\ isGzip file img
  /\ Tar.looksLikeRootkit (gunzip file img).
```

This predicate indicates that there is a deleted file within the file system image img, it is a gzip-compressed file, and the result of decompressing the file is a tar archive that is consistent with a rootkit.

The File type represents metadata about the file, including its size, the location of the file's content, and whether or not the file is deleted. The isOnDisk predicate establishes that the metadata given in file exists in img. The definition of the isOnDisk predicate is specific to the Ext2 file system. We leave the modular specification of other file systems to future work.

The isGzip predicate is a simple signature-based check of the contents of the file. This predicate examines the actual file content from img, where the location of the content is determined by file. The decision to refer to file content by indirection to img, as opposed to storing a copy of the file content in file, makes it easier to avoid duplication of the content in the resulting proof term's witness for the existential.

The Tar.looksLikeRootkit predicate examines the structure of a tar file, and tests whether two or more names of archive entries are on a blacklist, reflecting Borland's discussion. Borland's report does not contain an analysis of the malicious executables within the tar file. We discuss the use of gunzip below.

B. Proof Outline

If there were no limits on the size of data that could be handled by Coq, we would like to prove:

```
Lemma attempt1 : borland_rootkit honeynet_img.
```

where honeynet_img is a data structure holding the entire 259MB file system image. However, as discussed in the introduction, this data structure is many orders of magnitude larger than Cog can handle. Our second attempt is to identify a subset honeynet_img_partial of honeynet_img, and prove:

Lemma attempt2 : borland_rootkit honeynet_img_partial. This is useful in the presence of a monotonicity result of the form (recall that \sqsubseteq is the inclusion order on maps represented as functions):

```
Lemma borland_rootkit_mono :
 forall (img1 img2 : Img),
    img1 ⊑ img2 ->
    borland_rootkit img1 ->
    borland_rootkit img2.
```

Assuming a proof term inclusion for the order:

 $inclusion : honeynet_img_partial \sqsubseteq honeynet_img$

we would then have the following proof term for the original lemma attempt1 above:

```
borland rootkit mono
 honeynet_img_partial
 honeynet_img
 inclusion
 attempt2
: borland_rootkit honeynet_img.
```

Since honeynet_img, and consequently inclusion, cannot be defined in Coq, this final conclusion must be checked by a composition verifier rather than Coq. Additionally, the proof of honeynet_img_partial

□ honeynet_img involves running a simple external verifier that has access to the partial image used in Coq and the full file system image.

C. Decompression

It remains to prove attempt2. This proof is complicated by the presence of decompression in borland_rootkit (the forensics claim). There are two issues. The first is that a Coq coding of the gzip decompression algorithm is non-trivial to develop. The second is that the decompression algorithm uses the entire compressed input to produce the entire decompressed output, and the entire compressed input file is also too large to represent in Coq. This is unfortunate because the predicate Tar.looksLikeRootkit requires only part of the decompressed file, by analogy with the use of honeynet_img_partial above. It is possible to describe relationships between partial input and partial output for the decompression algorithm, but these relationships are particularly complex.

For these reasons, we rely on an external program to decompress the file. The external decompressor becomes part of the TCB, in addition to the Coq type checking kernel, the specification library, and other external verifiers. While not ideal, including decompression in the TCB seems to be a benign compromise: we believe that errors in forensic claims are more likely to be associated with specialized, domain-specific

tools and arguments rather than with standard decompression tools.

In addition to executing the decompression algorithm outside Coq, we also leave the decompression algorithm uninterpreted within the Coq specification and proof of the forensic claim. That is, the Coq script includes the declaration of a free variable for the decompression function:

```
Variable gunzip : File -> Img -> File.
```

Note that the File type may optionally include file content, and this is important for gunzip because the result of decompressing cannot normally be found in the file system image.

We have already seen that the uninterpreted gunzip function appears in the forensic claim borland_rootkit. In order to establish a property of the results of gunzip, we require a hypothesis about gunzip in the forensic claim. The hypothesis is that there is a subset gunzipped_partial of the decompressed data obtained from the compressed file file23 (the file for inode 23 in the Honeynet challenge image) within the file system image, written as follows:

```
gunzip_inclusion :
```

```
The proof of borland_rootkit is then based on factoring
```

it into the following lemma about the subsets honeynet_image_partial and gunzipped_partial of the file system image and the decompressed file respectively:

```
Lemma attempt3:
  isOnDisk file23 honeynet_image_partial
  /\ isDeleted file23
```

/\ isGzip file23 honeynet_image_partial.

/\ Tar.looksLikeRootkit gunzipped_partial.

Monotonicity results are used to extend the above lemma to larger file system images. For the first three predicates, monotonicity results resemble borland_rootkit_mono. For the last predicate, we show that Tar.looksLikeRootkit is monotone in its File argument:

```
Lemma looksLikeRootkit_mono :
  forall (f1 f2 : File),
    f1 ⊑ f2 ->
    Tar.looksLikeRootkit f1 ->
    Tar.looksLikeRootkit f2.
```

The individual monotonicity results are combined as:

Lemma borland_rootkit_mono_revised :

```
forall (img1 img2 : Img) (file f1 f2 : File),
  img1 \sqsubseteq img2 \rightarrow
  f1 □ f2 ->
  (isOnDisk file img1
   /\ isDeleted file
   /\ isGzip file img1
   /\ Tar.looksLikeRootkit f1) ->
  (isOnDisk file img2
   /\ isDeleted file
   /\ isGzip file img2
   /\ Tar.looksLikeRootkit f2).
```

Outside Coq, this monotonicity result can be used with the large honeynet_image to create the following proof term:

```
borland_rootkit_mono_revised
 honeynet_image_partial honeynet_image
  file23
  gunzipped_partial (gunzip file23 honeynet_image)
```

```
inclusion gunzip_inclusion
  attempt3 :
(isOnDisk file23 honeynet_image
/\ isDeleted file23
/\ isGzip file23 honeynet_image
/\ Tar.looksLikeRootkit (gunzip file23 honeynet_image))
Within Coq, we instead finalize the formalization of the forensic claim as:
Lemma borland_honeynet_final :
  forall (img : Img),
    honeynet_image_partial \subseteq img ->
        gunzipped_partial \subseteq gunzip file23 img ->
        borland_rootkit img.
Then the conclusion (borland_rootkit honeynet_image)
```

Then the conclusion (borland_rootkit honeynet_image) depends only on external verification of the two properties: inclusion:

```
honeynet_image_partial \sqsubseteq honeynet_image gunzip_inclusion : gunzipped_partial \sqsubseteq gunzip file23 honeynet_image
```

The external verifiers for these properties are part of the TCB for the verification architecture. The first property is trivial to check. The second property can easily be implemented using http://zlib.net/, which also becomes part of the TCB.

D. Coq Formalization

The Coq formalization of Borland's report has two components:

- (a) The specification of the forensic claim, including the definition of data structures for the Ext2 file system.
- (b) Procedures used in proof by reflection, and proofs of lem-

Code in (a) is part of the TCB, in addition to the Coq standard library definitions and the Coq type checking kernel, and is approximately 800 lines of code. Code in (b) is not part of the TCB, and is approximately 1,800 lines of code.

The proof of concept currently lacks integration with existing forensics search tools. For example, we have used simple custom tools to extract honeynet_image_partial and gunzipped_partial for insertion into Coq statements. These custom tools are not part of the TCB.

Verifying the entire development, including both the forensic claim and proofs of correctness, takes approximately 26 seconds. We use Coq's vm_compute tactic to normalize terms with the virtual machine, as opposed to the default normalization mechanism, for reasons of speed. The default normalization mechanism requires 267 seconds to complete the proof for attempt3, whereas the virtual machine mechanism completes the same proof in 4.6 seconds. The reported times are for Coq 8.4pl2 and Linux kernel 3.2.0, executing on a Xeon E3-1230 running at 3.20GHz with 16GB of RAM.

VI. ANALYSIS OF FORENSICS SPECIFICATIONS

If a forensics certificate includes a claim about a file system, it must inevitably include description of that file system. Such descriptions can be complex, and yet they must be trusted. In this section we discuss analysis of forensics specifications to

develop confidence in their correctness. We focus on specifications of heuristics used in the recovery of deleted files. Our results have been partially formalized in Coq.

Digital forensics tools do not necessarily limit themselves to a specification of a file system needed for a file system driver, referred to as a *standard specification* in the sequel. This is because it is useful to interpret data structures that are undefined, or invalid with respect to the standard specification. This additional effort may recover data that is hidden/secret, or may constitute proof of prior actions, e.g., possession of data at a certain time. Instances include: interpreting partially-overwritten file systems after a "quick format" has taken place, recovering deleted files, or recovering data deliberately hidden by anti-forensics tools [Garfinkel 2007].

If a forensics search recovers secret data, e.g., cryptographic keys or the names of conspirators, and learning the secret is sufficient, then there may be no need to provide evidence. On the other hand, if the purpose of a forensics search is to convince others that recovered data has not been fabricated by the search process or that the search process is thorough, then supporting evidence is required. For such evidence to be satisfactory, it must provide some meaning to otherwise undefined or invalid data structures. We refer to this as an extended specification in the sequel.

To illustrate, we sketch an extended specification for deleted files in the FAT file system.

A. Semantics of Deleted Files in the FAT File System

The FAT file system [Microsoft Corporation 2000] stores the contents of files in cluster chains, consisting of one or more clusters that may be contiguous or fragmented across the file system. The File Allocation Table (FAT) is a data structure that records both the allocation status of clusters and the order of clusters that make up a file. Conceptually, the FAT is a partial map FAT: $\mathbb{Z} \rightarrow \{\text{UN}, \text{TM}\} \cup \mathbb{Z}$. For a cluster number n, if FAT(n) = UN, then cluster n is unallocated. If FAT(n) = $n' \in \mathbb{Z}$, then cluster n is allocated and it is followed by cluster n' in a cluster chain. If FAT(n) = TM, then cluster n is allocated and is the terminal entry in a cluster chain. A FAT should not have occurrences of UN in cluster chains. A directory entry in a FAT file system image contains the filename, the file size, and the starting cluster number. A file system driver accesses a file's contents by calculating the cluster chain from the FAT.

Typically, when a file is deleted, the first byte of the filename is overwritten with a distinguished value (marking the directory entry as unallocated), and the entire cluster chain is marked as unallocated in the FAT. A side effect of the FAT representation is that the cluster chain is overwritten by the deallocation.

An extended specification for the existence of a deleted file in a FAT file system then has to: (a) identify an unallocated directory entry, yielding partial file name and file size; and (b) identify a cluster chain storing the file contents.

It is reasonable to justify (a) either by exhibiting a path from the root directory to the directory entry, or by showing that the contents matches the form of a directory entry.

For (b), Carrier [2005] describes two simple heuristics for choosing a cluster chain for deleted files. To see the

heuristics for a deleted file, consider a cluster chain map cluster : $[0,L) \to \mathbb{Z}$ of length $L \triangleq \lceil (\text{fileSize/clusterSize}) \rceil$. We insist that cluster(0) = init is the starting cluster number given in the directory entry for non-empty files, and that all clusters in the chain are unallocated:

$$\forall 0 \le i < \mathsf{L}. \; \mathsf{FAT}(\mathsf{cluster}(i)) = \mathsf{UN}$$

The specification for the first heuristic states that the cluster chain is contiguous:

$$\forall 0 \le i < \mathsf{L}. \ \mathsf{cluster}(i) = \mathsf{init} + i$$

The second heuristic generalizes the first. The specification allows the cluster chain to be fragmented, but each fragment must be filled with allocated clusters:

$$\begin{aligned} \forall 0 \leq i < \mathsf{L}. \\ \mathsf{cluster}(i) = \\ \mathsf{init} + i + |\{j \mid 0 \leq j < \mathsf{cluster}(i) \land \mathsf{FAT}(\mathsf{init} + j) \neq \mathsf{UN}\}| \end{aligned}$$

Casey [2004] demonstrates that both of these heuristics are used in forensic tools, and yield different results.

B. Analysis of the Semantics of Deleted Files

Since there are many possible extended specifications for recovery of information from deleted files, or more generally undefined and invalid data structures, how do we know whether a particular choice of specification is reasonable?

One approach is to ask whether an undeletion heuristic reflects a sequence of file operations on a file system that could have taken place. However, in fragmented file systems the undeletion heuristics described above may recover files incorrectly, despite the existence of a file system and a deletion operation that could have led to the file system that is being analyzed.

Rather than abstract operations, we consider *patches* to an image. A patch is intended to restore an undefined or invalid data structure to a valid state. Patches provide a deterministic, concrete explanation of changes. We represent a patch as a partial map Δ from offsets to bytes, and write $\operatorname{Img} \oplus \Delta$ for the partial map where Δ updates Img .

The question is now, if the extended specification justifies recovery of a deleted file from $\mathsf{Img}_2,$ does there exist a partial map Δ such that the file exists in $\mathsf{Img}_2 \oplus \Delta$ with respect to the standard specification? This property holds for the extended specifications described above. Diagrammatically, we have the following.

$$\begin{array}{c|c} \operatorname{Img}_2 \oplus \Delta \leftarrow ---- \operatorname{Img}_2 \\ \text{fileExists} & & & \operatorname{fileExistsDeleted} \\ \text{(filename, content)} & & & \text{(filename, content)} \end{array}$$

Without any constraint, of course, patching is too powerful to be useful. The entirety of the disk can be overwritten!

The simplest form of constraint limits the size of a patch. For example, a patch for the recovery of a deleted (but not overwritten) JPEG image file would be suspicious if it modified more than a few hundred bytes. Nevertheless, constraints

on patch size may not identify patches that modify, e.g., EXIF metadata in a JPEG image file (to suggest that a photo was taken at a particular location and time), or the contents of a spreadsheet.

For this reason, it is important to understand the semantic content of a patch. Often the domain of a patch provides an adequate approximation. In the case of the extended specifications described above, the patch Δ modifies: a single byte within the directory entry for the recovered file, and parts of the FAT. This is sufficient to argue that the contents of the file has not been manufactured by the forensics process.

We have developed a standard specification of the FAT16² file system, and an extended specification for the existence of deleted files following the first heuristic described above, in Coq. The specifications have been tested against sample file system images. To analyze the extended specification, we have defined a function to construct the patch Δ described above, given a reference to a deleted file within a FAT16 file system. We are in the process of formalizing the proof that a patch Δ for a deleted file (with respect to our extended specification) can be applied to the file system to yield a new file system where the file exists (with respect to our standard specification). In these proofs, tight constraints are needed on values in Δ to ensure that the file system is not corrupted, e.g., Δ must not modify the metadata that determines the size of entries in the File Allocation Table, and must not create entries in the File Allocation Table that are out of range.

VII. RELATED WORK

In this section we describe related work in digital forensics and theorem proving.

A. Declarative Models of Forensics

Stallard and Levitt [2003] describe a declarative encoding of data invariants and a decision tree format to codify the deductions performed by a forensic examiner.

Leigland [2004] discusses the effectiveness of forensics procedures against attackers in the context of a formal model. Carrier and Spafford [2006] provide a general model, incorporating history, to compare digital forensics methodologies, but do not consider specifications of evidence. Kahvedžić and Kechadi [2011] explores a semantic model of evidence using an existing forensics ontology.

van den Bos and van der Storm [2011] pioneer the toolindependent specification of file formats for creation of file recognizers for forensics purposes.

B. Validation of Computer Forensics Software and Results

Guo et al. [2009] develop and classifies detailed requirements for forensic tool testing. Lyle [2008] describes undesirable and inconsistent behavior of forensics tools. This has led to a subsequent program of testing [Lyle 2010]. The Scientific Working Group on Digital Evidence [2013] identify soundness problems in the output *and* interpretation of forensics tools, as well as completeness issues discussed in section III.

²FAT file systems may use 12, 16, or 32 bits for an entry in the File Allocation Table, and it is simpler to formalize just one variant, because the semantics of some metadata depends on the size of entries.

C. Proof Generation

Proof by Reflection: In section IV, we described the construction of proofs in forensic certificates via proof by reflection. This technique has been used in computationally-intensive formalizations, e.g., Gonthier [2007]. We have not yet investigated the use of architectures developed to assist with reflection Gonthier and Mahboubi [2010]; Malecha et al. [2013]. Chaieb and Nipkow [2008] argue that decision procedures used in proof by reflection should be abstract enough to share between theorem provers; the goal of reducing dependency on a particular theorem prover is relevant to forensic certificates.

Runtime Performance: To improve the performance of proof checking within Coq, Grégoire and Leroy [2002] show how to perform strong reduction (reduction under λ -abstractions) on a variant of the ZAM abstract machine (for the Objective Caml bytecode interpreter) using symbolic weak reduction and a readback scheme. Boespflug [2010]; Boespflug et al. [2011] describe recent work on untyped Normalization by Evaluation Berger et al. [1998] for Coq that compiles to Objective Caml programs.

Our formalization described in section V uses the implementation of binary integers in the Coq standard library. The extension of Coq with machine integers and persistent arrays Armand et al. [2010] has potential to improve the runtime performance of our formalization.

Richer Programming Models: Coq's type theory is strongly normalizing and stateless, and so it can be awkward to encode some computational procedures. Several recent works Claret et al. [2013]; Ziliani et al. [2013] have shown how computation in richer programming models (including, e.g., non-termination and state) can be reflected into Coq.

D. Verified SAT Solvers and Certificates

The forensic certificate architecture closely resembles that of SAT solver certificates. A SAT solver performs a computationally-intensive search for solutions, and produces a certificate for either a solution or a proof that the formula is unsatisfiable Darbari et al. [2010]. The certificate is verified by independent software. The code for the verifier, the TCB, is smaller and simpler than the code of the solver.

Two approaches have been used to integrate SAT solving with the Coq theorem prover. The first Lescuyer and Conchon [2008, 2009]; Lescuyer [2011] defines a SAT solver in Coq and establishes its correctness, i.e., proof by reflection is used in the search. The second, Darbari et al. [2010]; Armand et al. [2011], uses external SAT solvers for search, and then verifies the witnesses within Coq. The verification is conducted by certified code, i.e., proof by reflection is used in the verification. The latter approach avoids the need to certify the complex optimizations used in a SAT solver and the limitations of the runtime systems in existing theorem provers. Our forensic certificate architecture follows the latter approach.

One glaring dissimilarity between SAT solver certificates and our forensic certificate architecture lies in the treatment of negation. For SAT solver certificates, unsatisfiability is witnessed by a resolution proof. For forensic certificates, as discussed in subsection III-C, the absence of occurrences of

a property in a large interval of an image may be dealt with using external verifiers in conjunction with deduction using traditional theorem provers. The external verifiers may, of course, be verified using traditional program verification techniques or extracted from certified implementations.

VIII. CONCLUSION AND FURTHER WORK

The end goal of this research is trustworthy digital forensics. Practitioners and researchers have identified the opacity of software tools as a significant impediment in achieving this goal. Ongoing work in the community to address this situation has borrowed two important ideas from classical software engineering: (a) the clarification of software requirements for digital forensics tools, so as to identify what they are really doing, and (b) the facilitation of composition between tools to enable the construction of complex software artifacts from simpler pieces.

Our work borrows yet another idea from software construction: for software that is difficult to verify directly, one should focus instead on the correctness of individual executions. This has led us to design an architecture for forensic certificates that can be validated independently of the tools that created them in the first place.

In this paper, we have explored the challenges of applying this idea to the domain of digital forensics, in particular file system forensics. In the process, we have been forced to clarify the semantics of file system specifications and the trust relationships that are often left implicit in presenting the results of forensics analysis. Our case study from a forensics challenge provides some evidence for the viability of our approach.

We have introduced a novel approach for the specification and analysis of forensic data-recovery heuristics based on providing patches that restore data structures. We have discussed this in the context of recovering deleted files. More generally, forensic certificates containing patches (with semantic constraints) can explain forensics results that do not have commonplace operations. As two examples:

- A forensics search tool may find a partially-overwritten file
 in a disk image and provide a patch that fills in the missing
 data. The missing data might be taken from an older copy of
 the file found in a backup. The patch can describe precisely
 how much of the file is present on the original disk and how
 much is reconstructed from the backup.
- A simple anti-forensics tool that changes the size of clusters in the metadata can make a file system appear corrupt. A forensics search tool can create a patch that undoes the alteration and justifies that the change is consistent with other information in the file system. In other cases, tools may show that no such patch is possible.

We intend this paper as part of an ongoing research program to encompass other areas of digital forensics such as timeline analysis and memory forensics.

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